

List Of All Mathematical Formulas

The Universe in Equations: Your Guide to the Essential List of All Mathematical Formulas

Mathematics is the language of the universe. From the spiral of a galaxy to the rhythm of your heartbeat, mathematical formulas provide the framework for understanding how our world works. However, for students, professionals, and lifelong learners alike, keeping track of these essential tools can feel overwhelming. This comprehensive guide provides a curated **list of all mathematical formulas** you are likely to encounter, organized by discipline for easy reference. Whether you are preparing for an exam, brushing up on your skills, or simply marveling at the elegance of numbers, this resource is designed to be your go-to companion. Mastering this **list of all mathematical formulas** is not about rote memorization; it is about understanding the relationships that govern reality.

Why a Comprehensive List Matters

Before diving into the equations, it is important to understand why a compiled **list of all mathematical formulas** is more than just a cheat sheet. Formulas are shortcuts—they encapsulate complex logical relationships into a single, repeatable expression. Having a structured reference allows you to see connections between different branches of mathematics. For example, the area of a circle (geometry) connects to calculus through integration, and probability distributions rely heavily on algebraic functions. A well-organized list helps build this mental map, turning abstract symbols into intuitive knowledge.

Foundational Arithmetic and Basic Algebra

Every complex equation is built upon the bedrock of simple operations. This section of our **list of all mathematical formulas** covers the non-negotiable basics that underpin all higher mathematics.

Properties of Real Numbers

- **Commutative Property:** $a + b = b + a$ and $a \times b = b \times a$
- **Associative Property:** $(a + b) + c = a + (b + c)$ and $(a \times b) \times c = a \times (b \times c)$
- **Distributive Property:** $a(b + c) = ab + ac$
- **Identity Elements:** $a + 0 = a$ and $a \times 1 = a$
- **Inverse Elements:** $a + (-a) = 0$ and $a \times (1/a) = 1$ (where $a \neq 0$)

Essential Algebraic Formulas

Algebra is the language of generalization. These formulas allow you to solve for unknowns and manipulate expressions. Any reliable **list of all mathematical formulas** must include these core identities:

- **Quadratic Formula:** $x = [-b \pm \sqrt{b^2 - 4ac}] / 2a$ (for solving $ax^2 + bx + c = 0$)
- **Difference of Squares:** $a^2 - b^2 = (a - b)(a + b)$
- **Perfect Square Trinomials:** $(a + b)^2 = a^2 + 2ab + b^2$ and $(a - b)^2 = a^2 - 2ab + b^2$
- **Sum and Difference of Cubes:** $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ and $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
- **Laws of Exponents:** $a^m \times a^n = a^{m+n}$; $a^m / a^n = a^{m-n}$; $(a^m)^n = a^{m \times n}$

- **Logarithmic Identities:** $\log_b(xy) = \log_b x + \log_b y$; $\log_b(x/y) = \log_b x - \log_b y$; $\log_b(x^n) = n \log_b x$

Geometry: Measuring the Physical World

Geometry brings mathematics into the realm of shape, space, and dimension. These formulas are crucial for architecture, engineering, design, and everyday problem-solving. A complete **list of all mathematical formulas** for geometry must address both two-dimensional and three-dimensional figures.

Two-Dimensional Shapes

- **Perimeter of a Rectangle:** $P = 2(l + w)$
- **Area of a Rectangle:** $A = l \times w$
- **Area of a Triangle:** $A = \frac{1}{2} \times b \times h$
- **Area of a Circle:** $A = \pi r^2$
- **Circumference of a Circle:** $C = 2\pi r$
- **Pythagorean Theorem:** $a^2 + b^2 = c^2$ (for right triangles)
- **Area of a Trapezoid:** $A = \frac{1}{2} \times (b_1 + b_2) \times h$

Three-Dimensional Solids

- **Volume of a Cube:** $V = s^3$
- **Volume of a Rectangular Prism:** $V = l \times w \times h$
- **Volume of a Cylinder:** $V = \pi r^2 h$
- **Volume of a Sphere:** $V = (4/3)\pi r^3$
- **Volume of a Cone:** $V = (1/3)\pi r^2 h$
- **Surface Area of a Sphere:** $SA = 4\pi r^2$
- **Surface Area of a Cylinder:** $SA = 2\pi r^2 + 2\pi rh$

Trigonometry: The Study of Angles

Trigonometry is essential for understanding periodic phenomena, waves, navigation, and the relationship between angles and sides of triangles. No **list of all mathematical formulas** is complete without these fundamental trigonometric identities.

Basic Trigonometric Ratios

- **Sine:** $\sin(\theta) = \text{Opposite} / \text{Hypotenuse}$
- **Cosine:** $\cos(\theta) = \text{Adjacent} / \text{Hypotenuse}$
- **Tangent:** $\tan(\theta) = \text{Opposite} / \text{Adjacent}$

Key Trigonometric Identities

- **Pythagorean Identity:** $\sin^2(\theta) + \cos^2(\theta) = 1$
- **Reciprocal Identities:** $\csc(\theta) = 1/\sin(\theta)$; $\sec(\theta) = 1/\cos(\theta)$; $\cot(\theta) = 1/\tan(\theta)$
- **Double Angle Formulas:** $\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$; $\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta)$
- **Law of Sines:** $a/\sin(A) = b/\sin(B) = c/\sin(C)$
- **Law of Cosines:** $c^2 = a^2 + b^2 - 2ab \cos(C)$

Calculus: The Mathematics of Change

Calculus revolutionized mathematics by allowing us to study motion, change, and accumulation. It is divided into differential calculus (rates of change) and integral calculus (accumulation). A thorough **list of all mathematical formulas** must address the fundamental tools of calculus.

Limits and Continuity

- **Limit Definition of Derivative:** $f'(x) = \lim_{h \rightarrow 0} [f(x+h) - f(x)] / h$
- **Basic Limit Laws:** $\lim_{x \rightarrow a} [f(x) + g(x)] = \lim f(x) + \lim g(x)$

Differentiation Rules

- **Power Rule:** $d/dx (x^n) = n x^{n-1}$
- **Product Rule:** $d/dx [f(x)g(x)] = f'(x)g(x) + f(x)g'(x)$
- **Quotient Rule:** $d/dx [f(x)/g(x)] = [f'(x)g(x) - f(x)g'(x)] / [g(x)]^2$
- **Chain Rule:** $d/dx [f(g(x))] = f'(g(x)) g'(x)$
- **Derivatives of Trig Functions:** $d/dx \sin(x) = \cos(x)$; $d/dx \cos(x) = -\sin(x)$
- **Derivative of the Natural Log:** $d/dx \ln(x) = 1/x$

Integration Formulas

- **Power Rule for Integration:** $\int x^n dx = x^{n+1}/(n+1) + C$ ($n \neq -1$)
- **Fundamental Theorem of Calculus:** $\int_a^b f(x) dx = F(b) - F(a)$
- **Integration by Parts:** $\int u dv = uv - \int v du$
- **Basic Trig Integrals:** $\int \sin(x) dx = -\cos(x) + C$; $\int \cos(x) dx = \sin(x) + C$

Linear Algebra and Vectors

Linear algebra extends algebra into multiple dimensions. It is the backbone of computer graphics, data science, and physics. An exhaustive **list of all mathematical formulas** in this domain includes operations on vectors and matrices.

Vector Operations

- **Dot Product:** $a \cdot b = |a||b|\cos(\theta) = a_1b_1 + a_2b_2 + a_3b_3$
- **Cross Product:** $a \times b = |a||b|\sin(\theta) \hat{n}$
- **Magnitude of a Vector:** $|v| = \sqrt{v_1^2 + v_2^2 + v_3^2}$

Matrix Formulas

- **Matrix Multiplication:** $(AB)_{ij} = \sum_k A_{ik} B_{kj}$
- **Determinant of a 2x2 Matrix:** $\det([a \ b; c \ d]) = ad - bc$
- **Inverse of a 2x2 Matrix:** $A^{-1} = (1/\det(A)) [d \ -b; -c \ a]$

Probability and Statistics

In an age of data, probability and statistics are more important than ever. This section of our **list of all mathematical formulas** covers the essential tools for analyzing uncertainty and variability.

Descriptive Statistics

- **Mean:** $\bar{x} = (\sum x_i) / n$
- **Variance:** $\sigma^2 = \sum (x_i - \bar{x})^2 / n$
- **Standard Deviation:** $\sigma = \sqrt{\sigma^2}$
- **Z-Score:** $z = (x - \mu) / \sigma$

Probability Rules

- **Probability of an Event:** $P(A) = \text{Number of favorable outcomes} / \text{Total number of outcomes}$
- **Conditional Probability:** $P(A|B) = P(A \cap B) / P(B)$
- **Bayes Theorem:** $P(A|B) = [P(B|A) P(A)] / P(B)$
- **Binomial Probability:** $P(X = k) = C(n, k) p^k (1-p)^{n-k}$
- **Expected Value:** $E(X) = \sum x_i P(x_i)$